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NUMERICAL EVALUATION OF SPECIAL FUNCTIONS

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ABSTRACT. This document is an excerpt from the current hypertext version of an article that appeared in Walter Gautschi (ed.), *Mathematics of Computation 1943–1993: A Half-Century of Computational Mathematics*, Proceedings of Symposia in Applied Mathematics 48, American Mathematical Society, Providence, RI 02940, 1994. The symposium was held at the University of British Columbia August 9–13, 1993, in honor of the fiftieth anniversary of the journal *Mathematics of Computation*.

The original abstract follows.

Higher transcendental functions continue to play varied and important roles in investigations by engineers, mathematicians, scientists and statisticians. The purpose of this paper is to assist in locating useful approximations and software for the numerical generation of these functions, and to offer some suggestions for future developments in this field.

6. Testing and Library Construction

In this section we list articles and books that provide general observations on the testing of software and/or the construction of software libraries for the special functions. For information on individual libraries see §3.

[**Cod74**], [**Cod76**], [**Cod82**], [**Cod84b**], [**Cod85**], [**CS91**], [**Eva74**, especially pp. 275–301 and 357–435], [**Ful77**], [**Gaf88**], [**Kuk71**], [**LMS73a**], [**LMS73b**], [**Mos89**], [**PTVF92**, example books], [**Ric83**], [**Sch76**], [**SL73**].

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[1] /nesf/Sect0/Sect0.html

[2] /nesf/Sect5-14/Sect5-14.html

[3] /nesf/Sect7/Sect7.html

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