# OP-SFNET - Volume 32, Number 2 - March 15, 2025

# The Electronic News Net of the SIAM Activity Group on Orthogonal Polynomials and Special Functions

http://math.nist.gov/opsf

OP-SF Net is distributed to OPSF Activity Group members and non-members alike through the OP-SF Talk listsery.

If you are interested in subscribing to the Newsletter and/or OP-SF Talk, or if you would like to submit a topic to the Newsletter or a contribution to OP-SF Talk, please send an email to the OP-SF Net Editors.

#### **Editors**:

Howard S. Cohl howard.cohl@nist.gov Sarah Post spost@hawaii.edu

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#### Calendar of Events:

#### May 19-22, 2025

Constructive Functions 2025
Celebrating Ed Saff's 80<sup>th</sup> birthday
in conjunction with the 37<sup>th</sup> Shanks Lecture by Doron Lubinsky
Vanderbilt University, Nashville, Tennessee, USA
https://my.vanderbilt.edu/constructivefunctions2025/

#### June 23-28, 2025

Combinatorics around the *q*-Onsager algebra A celebration of the 70<sup>th</sup> birthday of Paul Terwilliger Kranjska Gora, Slovenia https://conferences.famnit.upr.si/event/15/overview

#### July 2-5, 2025

Third International Conference: Constructive Mathematical Analysis Selcuk University, Konya, Turkey

https://iccma.selcuk.edu.tr

# July 28-August 1, 2025

The Third Joint SIAM/CAIMS Annual Meetings (AN25)

Montréal, Québec, Canada

https://www.siam.org/conferences-events/siam-conferences/an25/

# August 19-22, 2025

Extremal Polynomials and Dynamical Systems

Carlsberg Academy, Copenhagen, Denmark

https://www.math.ku.dk/english/calendar/events/epds/

# July 8-18, 2026

Foundations of Computational Mathematics (FoCM 2026), University of Vienna, Vienna, Austria https://focm-society.org/

Workshop related to SIAG/OPSF:

Session, Date yet unknown: Orthogonal Polynomials and Special Functions

Organizers: "are to be confirmed."

Topic #1 — OP - SF Net 32.2 — March 15, 2025

From: OPSFA Steering Committee

Subject: Announcement: OPSFA-18 to be held at Doshisha University, Kyoto, Japan

Dear OPSF members,

We are happy to announce that after careful deliberation, the OPSFA Steering Committee has decided to accept the proposal from Doshisha University, Kyoto, Japan to host OPSFA-18 from August 17-21, 2026. The organizing committee members have been proposed to include at least: Satoshi Tsujimoto (Chair, Kyoto University), Hiroshi Miki (Co-Chair, Doshisha University), Yoshitsugu Takei (Doshisha University), and Teruhisa Tsuda (Aoyama University). Presentations are expected to be held in Hardy Hall and some other lecture rooms at Doshisha University, Kyoto, Japan. The estimated registration fee is expected to be between US\$300-400 and for students US\$150-200. For more information about Doshisha University see the following link:

https://www.doshisha.ac.jp/en/information/imadegawa/muromachi\_map/

Congratulations to the team from Doshisha University!

Best regards, OPSFA Steering Committee,

Luc Vinet, Peter Clarkson, Christoph Koutschan, Ana Loureiro and Howard Cohl

Topic #2 — OP - SF Net 32.2 — March 15, 2025

From: Jacob Stordal Christiansen (jacob\_stordal.christiansen@math.lth.se)

and Henrik Laurberg Pedersen (henrikp@math.ku.dk)

Subject: Announcement: "Extremal Polynomials and Dynamical Systems" in Copenhagen, Denmark

Announcement: International Conference on "Extremal Polynomials and Dynamical Systems"

We are pleased to announce the international conference "Extremal Polynomials and Dynamical Systems," taking place August 19-22, 2025, at the historic Carlsberg Academy in Copenhagen, Denmark.

This conference aims to bring together researchers from diverse areas related to **Approximation Theory** and **Dynamical Systems** to create collaboration and the exchange of ideas.

The program features 10 plenary talks by leading international experts, including:

- Bernhard Beckermann (University of Lille, France),
- Jonathan Breuer (Hebrew University of Jerusalem, Israel)
- Xavier Buff (University of Toulouse, France),
- Benjamin Eichinger (Lancaster University, UK),
- **Thomas Gauthier** (University Paris-Saclay, France),
- Luna Lomonaco (IMPA, Brazil),
- Andrei Martinez-Finkelshtein (Baylor University, USA and University of Almeria, Spain),
- Yusuke Okuyama (Kyoto University, Japan),
- Fredrik Viklund (KTH, Sweden), and
- Saeed Zakeri (City University of New York, USA).

For more details, visit the conference homepage: https://www.math.ku.dk/english/calendar/events/epds/.

#### Scientific Committee:

- Jacob Stordal Christiansen (Lund University)
- Christian Henriksen (Technical University of Denmark)
- Henrik Laurberg Pedersen (University of Copenhagen)
- Carsten Lund Petersen (University of Copenhagen)
- Eva Uhre (Roskilde University)

We look forward to welcoming you to Copenhagen!

Topic #3 — OP - SF Net 32.2 — March 15, 2025

From: Ryan W. Matzke (ryan.w.matzke@vanderbilt.edu)

Subject: Announcement: Deadlines: "Constructive Functions 2025" in Nashville, Tennessee

# **Constructive Functions 2025**

in conjunction with the

37<sup>th</sup> Annual Shanks Lecture
Celebrating Ed Saff's 80<sup>th</sup> birthday

Nashville, Tennessee May 19-22, 2025

https://my.vanderbilt.edu/constructivefunctions2025/ constructivefunctions2025@gmail.com We are pleased to send out the fourth announcement for the Constructive Functions 2025 conference. If you would like to contribute a talk, register for the conference, or find hotels at a negotiated price for the conference please visit: https://my.vanderbilt.edu/constructivefunctions2025/

# Important deadlines (with links):

- Application for Travel Support: March 15, 2025
   https://my.vanderbilt.edu/constructivefunctions2025/registration/support-requests/
- Abstract Submission Deadline: April 1, 2025
   https://my.vanderbilt.edu/constructivefunctions2025/current-courses/
- Registration Deadline: April 1, 2025 https://my.vanderbilt.edu/constructivefunctions2025/registration/registration/

The **37**<sup>th</sup> **Shanks Lecture** will be delivered by Professor Doron Lubinsky (Georgia Institute of Technology). The meeting will also provide an excellent opportunity to celebrate **Professor Ed Saff's 80**<sup>th</sup> **birthday**.

The prestigious Shanks Lecture Series is organized annually by the Department of Mathematics in honor of Baylis and Olivia Shanks. The late Professor Baylis Shanks was chairman of the Department from 1956 through 1969. A list of previous Shanks Conferences and Lecturers can be found here.

Students, early career researchers, women, and other minorities are especially encouraged to attend this conference. We have applied for funding from the NSF and are waiting to hear if we can offer some support for such participants.

# **Invited Speakers**:

- Doron Lubinsky, Shanks Lecturer, Georgia Institute of Technology, USA
- Peter Dragnev, Purdue University Fort Wayne, USA
- Arno Kuijlaars, KU Leuven, Belgium
- Ana Loureiro, University of Kent, UK
- Andrei Martínez-Finkelshtein, Baylor University, USA
- Ana Matos, Universite de Lille, France
- Jill Pipher, Brown University, USA
- Ian Sloan, University of New South Wales, Australia
- Eitan Tadmor, University of Maryland, USA
- Nick Trefethen, Harvard University, USA

#### Organizing Committee:

- Stephen Gardiner, University College Dublin
- Doug Hardin, Vanderbilt University
- Liudmyla Kryvonos, Vanderbilt University
- Juliette LeBlond, INRIA Sophia Antipolis Méditerranée
- Doron Lubinsky, Georgia Institute of Technology
- Ryan Matzke, Vanderbilt University
- Igor Pritsker, Oklahoma State University
- Mihai Putinar, University California Santa Barbara
- Maya Stoyanova, Sofia University
- Robert Womersley, University of New South Wales

Maxim Yattselev, IUPUI

#### Scientific Committee:

- Laurent Baratchart, INRIA Sophia Antipolis Méditerranée
- Sergiy Borodachov, Towson University
- Peter Boyvalenkov, Bulgarian Academy of Sciences
- Kathy Driver, University of Cape Town
- Guillermo López Lagomasino, Universidad Carlos III de Madrid
- Xin Li, University of Central Florida
- Igor Shevchuk, Taras Shevchenko National University of Kyiv
- Nikos Stylianopoulos, University of Cyprus
- Natalia Zorii, National Academy of Sciences of Ukraine

We hope to see you in May!

Best wishes,
The Constructive Functions 2025 Organizing Committee

Topic #4 — OP - SF Net 32.2 — March 15, 2025

From: Howard Cohl (howard.cohl@nist.gov), Sarah Post (spost@hawaii.edu), Kerstin Jordaan (jordakh@unisa.ac.za) and Tom Trogdon (trogdon@uw.edu)

Subject: Announcement: SIAG/OPSF Minisymposia at SIAM/CAIMS Annual Meetings in Montréal, Canada

We are very happy to report that thanks to the hard work of the elected officers for our activity group we have a strong showing of 6 minisymposia proposed for the upcoming Third Joint SIAM/CAIMS Annual Meetings (AN25) in Montréal. Beginning on January 1<sup>st</sup>, 2025, when their elected period started for SIAG/OPSF, Howard Cohl, Kerstin Jordaan and Tom Trogan contacted and identified organizers for the following OPSF related minisymposia. These minisymposia were all successfully submitted to SIAM prior to the short deadline of February 10, 2025 and the schedule will be available during the first week of April.

Assuming these minisymposia are accepted, when the program is posted, they will all be listed on the conference website as being sponsored by the SIAM Activity Group on OPSF.

# Proposed SIAG/OPSF minisymposia:

# 1. Spectral Graph Theory, Orthogonal Polynomials, and Quantum Computing

Organizers: Anastasiia Minenkova (University of Hartford) and Harmony (Hanmeng) Zhang (Worcester Polytechnic Institute)

List of Speakers:

- (a) Rachel Bailey, Bentley College, USA
  Title: Orthogonal Polynomials and Perfect State Transfer
- (b) Luc Vinet and Pierre-Antoine Bernard, Université de Montréal, Canada; Title: A dynamical algebra of protocol-induced transformations on Dicke states
- (c) Pierre-Antoine Bernard\*, Ismaël Bussière \*, Roberto Floreanini $^{\dagger}$  and Luc Vinet\* \*Université de Montréal, Canada;  $^{\dagger}$ INFN Trieste, Italy; Title: Currents in non-equilibrium steady states of open inhomogeneous XX-spin chains

(d) Anastasiia Minenkova, University of Hartford, West Hartford, CT, USA Title: Early State Exclusion

(e) Christino Tamon, Clarkson University, USA Title: State Transfer in Chiral Quantum Walks

(f) Ada Chan, York University, Canada Title: Multiple state transfer

(g) Chris D. Godsil, University of Waterloo, Canada Title: TBD

(h) Harmony Zhan, Worcester Polytechnic Institute, USA
Title: Simple Quantum Coins Enable Pretty Good State Transfer on Every Hypercube

(i) Vita Borovyk, University of Cincinnati, USA

Title: Distance Measures for Quantum States and Channels: Properties and Applications

(j) Nobuaki Obata, Tohoku University, Japan Title: Partial Chebyshev Polynomials and Fan Graphs

(k) Tiju John\*, Repana Devendra† and Sumesh K.‡
\*University of Arizona, USA; †IIT Bombay, India; ‡Indian Institute of Technology Madras, India
Title: What Is a Gaussian Channel, and When Is It Physically Implementable Using a Multiport
Interferometer?

# 2. Digital Mathematical Content on the Web

Organizers: Howard Cohl (NIST) and Edward Dunne (Mathematical Reviews) List of Speakers:

- (a) Howard Cohl, Applied and Computational Mathematics Division, NIST, Gaitherburg, MD, USA Title: Recent and future activities of the NIST Digital Library of Mathematical Functions Project
- (b) Edward Dunne, Mathematical Reviews, American Mathematical Society, Ann Arbor Michigan, USA

Title: Accessing mathematics using MathSciNet

- (c) Deyan Ginev, arXiv, Cornell Tech, New York, NY, USA Title: arXiv.org as HTML Papers the next 20.25%
- (d) Moritz Schubotz, FIZ Karlsruhe-Leibniz-Institut für Informationsinfrastruktur, Berlin, Germany Title: Mathematical Research Data in zbMATH Open, Wikipedia, and Beyond
- (e) Blaec Bejarano, CoCalc Title: CoCalc by SageMath
- (f) Jen Paulhus, Department of Mathematics and Statistics, Mount Holyoke College, South Hadley, MA, USA

Title: LMFDB: the joys and challenges of developing a mathematical database.

(g) Christelle Vincent, Department of Mathematics and Statistics, University of Vermont, Burlington, VT, USA

Title: Exploring angle ranks using the LMFDB and a brief introduction to code4math.

(h) Bonita Saunders, Applied and Computational Mathematics Division, National Institute of Standards and Technology, Gaithersburg, Maryland, USA
Title: NIST DLMF Tables Project

#### 3. Hypergeometric Series and Their Applications

Organizers: Maddie Dawsey (U Texas at Tyler) and Fang-Ting Tu (Louisiana State University) List of Speakers:

- (a) Ling Long, Louisiana State University
  Title: Applications of Hypergeometric Functions to Modular Forms
- (b) Neelam Saikia, Indian Institute of Technology Bhubaneswar Title: Distributions of Gaussian Hypergeometric Functions
- (c) Rupam Barman, Indian Institute of Technology Guwahati Title: p-Adic Hypergeometric Functions and Certain Weight Three Newforms
- (d) David P. Roberts, University of Minnesota, Morris Title: Hypergeometric Period Matrices
- (e) Armin Straub, University of South Alabama
  Title: Diagonal and Constant Term Representations of Sequences
- (f) Yifeng Huang, University of Southern California Title: RR-Type Identities from Zeta Functions over Quadratic Orders
- (g) Lin Jiu, Duke Kunshan University Title: Hankel Determinants and Jacobi Continued Fractions for q-Euler Numbers
- (h) Esme Rosen, Louisiana State University
  Title: Hypergeometric Functions and Modular Forms
- (i) Vyacheslav Spiridonov, National Research University Higher School of Economics, Moscow and Joint Institute for Nuclear Research, Dubna, Russia

  Title: A General Scheme of Hypergeometric Functions and Limiting Transitions Between Them
- (j) Cameron Franc, McMaster University
  Title: On densities of bounded primes for hypergeometric series

# 4. Orthogonal Polynomials and Special Functions in Modern Applications

Organizers: Peter Miller (University of Michigan) and Giorgio Young (University of Michigan) List of Speakers:

- (a) Robert Jenkins, University of Central Florida

  Title: Extreme focusing events in the semiclassical scaled focusing NLS hierarchy
- (b) Jonathan Stanfill, The Ohio State University
  Title: Asymptotic Analysis and Special Functions and Applications to Spectral Zeta Functions
- (c) Tom Trogdon, University of Washington Title: The Ultraspherical Rectangular Collocation Method and Its Convergence
- (d) Giorgio Young, University of Michigan
  Title: Rational Solutions to the Modified Korteweg-De Vries Equation

# 5. Special Functions with Applications in Number Theory and Combinatorics

Organizers: Lin Jiu (Duke Kunshan University)

List of Speakers:

- (a) Alexey Kuznetsov, York University
  Title: Zeros of the Deformed Exponential Function
- (b) Victor Moll, Tulane University

  Title: The Limiting Behavior of Zeros of a Family of Polynomials Coming from a Rational Integral
- (c) Nasser Saad, University of Prince Edward Island
  Title: On Meixner-Pollaczek polynomials and the Sturm-Liouville Problem

(d) Karl Dilcher, Dalhousie University
Title: Orthogonal Polynomials and Hankel Determinants for Certain Bernoulli and Euler Polynomials

# 6. Association scheme, orthogonal polynomials, and integrable systems

Organizers: Luc Vinet (CRM/Ivado) and Nicolas Crampé (Université de Tours)

List of Speakers:

(a) Riley Casper, California State University, Fullerton Title: Discrete Bispectrality and Pascal's Matrix

(b) Nicolas Crampé, Université de Tours Title: Bispectral Bivariate Polynomials

(c) Maxim Derevyagin, University of Connecticut Title: On indefinite orthogonal polynomials

(d) Alberto Grunbaum University of California, Berkeley
Title: The Darboux process and the ad conditions: a study case involving the Laguerre case

(e) Jacek Szmigielski, University of Saskatchewan Title: Euler-Bernoulli beam problem and non-commutative Stieltjes's continued fractions

(f) Quentin Labriet, CRM / Université de Montréal Title: Infinite Dimensional Representations of the Meta Hahn Algebra and Special Functions

(g) Lucia Morey, CRM / Université de Montréal Title: Algebraic Interpretation of Discrete Families of Matrix Valued Orthogonal Polynomials

(h) Sarah Post, University of Hawaïı

Title: Multivariate Racah Polynomials and their associated algebras

(i) Franco Saliola, CRM / Université du Québec à Montréal
 Title: Commutative subalgebras of symmetric groups and Hecke algebras arising from shuf-fling processes

(j) Paul Terwilliger, University of Wisconsin-Madison Title: The nucleus of a Q-polynomial distance-regular graph

(k) Jan Felipe van Diejen, Instituto de Matemáticas, Universidad de Talca Title: The Spectrum of the Finite Open XX Quantum Spin Chain with Transverse Magnetic Boundary Fields Via Orthogonal Polynomials

# 7. Computation of Special Functions

Organizers: Javier Segura and Amparo Gil (University of Cantabria) List of Speakers:

(a) Amparo Gil, University of Cantabria, Spain
Title: Improving the Quality of Numerical Software for Distribution Functions

(b) Robert Corless, Western University & University of Waterloo, Canada Title: Computation of Generalized Mathieu Functions

(c) Richard Slevinsky, University of Manitoba, Canada Title: FaFast Measure Modification of Orthogonal Polynomials Via Matrices with Displacement Structure

(d) Wietse Vaes, University of Washington, USA

Title: Special Functions and the Numerical Solution of Initial-Boundary Value Problems

### 8. Multivariate Approximation and Orthogonality

Organizers: Teresa Pérez (Universidad de Granada) and Miguel Piñar (Universidad de Granada) List of Speakers:

- (a) Luis Garza, Facultad de Ciencias, CUICBAS, Universidad de Colima, México Title: On Symmetric Multivariate Orthogonal Polynomials
- (b) Herbert Duenas-Ruiz, Universidad Nacional de Colombia, Sede Bogota Title: Particular Cases of Sobolev-Type Zernike Orthogonal Polynomials
- (c) Ana Foulquie-Moreno, Dep. of Mathematics, Universidade de Aveiro, Portugal Title: Applications of Quadratic Decomposition for Bivariate Orthogonal Polynomials
- (d) Amilcar Branquinho, Dep. of Mathematics, Universidade de Coimbra, Portugal Title: Lax-Type Pairs in the Theory of Bivariate Orthogonal Polynomials
- (e) Misael Marriaga, Dep. of Applied Mathematics, University Rey Juan Carlos, Madrid, Spain Title: Higher-Order Differential Operators Having Bivariate Orthogonal Polynomials As Eigenfunctions
- (f) Cleonice Bracciali, Dep. of Mathematics, IBILCE-UNESP, sede Sao Jose do Rio Preto, Brazil Title: Centrosymmetric and Reverse Matrices in Bivariate Orthogonal Polynomials
- (g) Manuel Manas, Dep. of Theoretical Physics, Universidad Complutense de Madrid, Spain Title: Multivariate Orthogonal Laurent Polynomials and Integrable Systems
- (h) Incoronata Notarangelo, Department of Mathematics "Giuseppe Peano", University of Torino, Italy

Title: Advances in Truncated Gaussian Quadrature Rules for Exponential Weights

- (i) Teresa E. Pérez, Institute of Mathematics IMAG, University of Granada, Spain Title: Bivariate Bernstein-Jacobi approximants for negative parameters
- (j) Miguel A. Piñar, Dept. of Applied Mathematics, University of Granada, Spain Title: On Classical Generalized Bivariate Symmetric Polynomials

# 9. Numerical methods in the theory of orthogonal polynomials and special functions

Organizers: Cade Ballew (University of Washington), Richard Mikaël Slevinsky (University of Manitoba) and James Bremer (University of Toronto)

List of Speakers:

- (a) James Bremer, University of Toronto Title: Airy phase functions
- (b) Cade Ballew, University of Washington
  Title: The Akhiezer iteration and an inverse-free solver for Sylvester matrix equations
- (c) Gabriel Hamm, University of Manitoba Title: Fast algorithms for Sobolev orthogonal polynomials
- (d) Kirill Serkh, University of Toronto
  Title: The Approximation of Singular Functions by Series of Non-Integer Powers

Topic #5 — OP - SF Net 32.2 — March 15, 2025

From: OP-SF Net Editors

Subject: Further remembrances of Masatoshi Noumi (1955–2024)

# Further Remembrances of Masatoshi Noumi (March 11, 1955—November 20, 2024)

Below are three remembrances of Masatoshi Noumi from four of his close colleagues:

Edwin Langmann and Junichi Shiraishi; Jasper Stokman; Tom Koornwinder.

\* \* \*

# Remembrance of Masatoshi Noumi

Edwin Langmann (langmann@kth.se) and Junichi Shiraishi (shiraish@ms.u-tokyo.ac.jp)

We are lucky to belong to the group of scientists who have closely interacted and worked with Masatoshi Noumi. He was passionate about mathematics, caring, encouraging, talented, wise, reliable; in short, and outstanding scientist, human being, and role model for many of us. We shared with him a passion for beautiful formulas related to Macdonald theory and its elliptic generalization due to Ruijsenaars. One of us (JS) has worked with him since 1992. Some years later, Masatoshi–san got busy with heavy administrative duties at Kobe University. Despite of these duties, Masatoshi–san managed to remain an outstanding research leader, collecting a group of scientists around hin in regular meetings, inspiring work, helping work to get finished by his kind and encouraging way, his interest, his helpful advice and feedback.

It was always fun to go to dinner with the participants after the seminar. We liked to drink wine with our meals, and Masatoshi-san would always remind us of the famous "Mimachi's Theorem": "The number of bottles of wine tonight is the number of us plus one." We always felt that we needed to recharge our energy to complete some great mathematical theorem, so we always did just that, eating, drinking and talking a lot.

The three of us met first in person at a wonderful meeting on elliptic integrable systems at the Lorentz Center in Leiden in 2013, realizing in discussions that we shared very close scientific interests. It took us until 2019 to find a productive way to collaborate, aided by Zoom, which we learned to use as a collaboration tool during covid time. Masatoshi Noumi was guest professor in Stockholm for a year starting in August 2020 which, despite covid and with the help of Zoom, turned out very productive. We finished papers but also discussed topics which has given us work for years to come — we try to keep working on these topics (in on–going work with Martin Hallnäs), and we trust there will be future papers developing Masatoshi–san's beautiful mathematics and ideas. We are missing and remembering him, trying to continue what we learned from him.

We both are theoretical physicists by education and have both worked on topics belonging to other research communities. Both of us therefore appreciate that the research community to which Masatoshisan belonged functions outstandingly well. It is well-grounded in good traditions, welcoming to newcomers (including us some time ago), encouraging, and not focusing on indicators of scientific success that can be measured in numbers but instead on intellectual content. We strongly believe that the atmosphere within a research community is to a large degree affected by the human qualities of its leaders. Masatoshi Noumi was a research leader with high standards in his work, who was not only very talented, but at the same time had outstanding human qualities. We think we are two of many who owe him a lot.

Masatoshi Noumi

Jasper Stokman (J.V.Stokman@uva.nl)



Figure 1: Tom Koornwinder and Masatoshi Noumi at my Ph.D. defense in Amsterdam, June 1998.

In the spring of 1994 a concentration period on Representation Theory and q-Special Functions took place in Leiden, The Netherlands. Masatoshi Noumi was giving a mini-course about the quantum group analogue of the Borel-Weil construction of the finite-dimensional irreducible representations of  $GL(n,\mathbb{C})$ , based on his joint paper [1] with Hirofumi Yamada and Katsuhisa Mimachi. I attended the mini-course as a master student, knowing that I would continue a couple of months later with a Ph.D. on quantum groups and q-special functions under the guidance of Tom Koornwinder. Masatoshi's patient and systematic style of presentation and his ability to clearly convey the main ideas made a big impression on me. As soon as I started as a Ph.D. student, I read their beautiful paper, which also contains the interpretation of little q-Jacobi polynomials as spherical functions on quantum odd-dimensional spheres, from front to back.

In 1992 Tom Koornwinder published a simultaneous generalisation of Macdonald polynomials and the Askey-Wilson polynomials [2], nowadays known as Koornwinder polynomials. The plan of my Ph.D. was to find similar multivariable analogs of some of the descendants of the Askey-Wilson polynomials in the q-Askey scheme, and interpret those as spherical functions on quantum homogeneous spaces. While working on the first half of the plan, Masatoshi's breakthrough paper [3] appeared in which he gave the first examples of Macdonald polynomials as spherical functions on quantum homogeneous spaces. The paper was sprinkled with beautiful new ideas and showed his mastery of all aspects of quantum groups known at that time: Drinfeld-Jimbo approach; Faddeev's approach motivated by quantum physics; and the non-commutative geometry approach by Majid. The second part of my Ph.D.-plan wouldn't have stood a chance without this paper and his followup work [4] with Mathijs Dijkhuizen and Tetsuya Sugitani realizing the Koornwinder polynomials as spherical functions on quantum complex Grassmannians. Joint with Mathijs Dijkhuizen, who stayed at that time for several years at Kobe University in the research group of Masatoshi, we extended the results from [4] to obtain a quantum group interpretation of multivariable big and little q-Jacobi polynomials.

To complete this project, I spent 10 weeks at Kobe University in 1997. Masatoshi showed kind interest in my work, but we did not have much chance to talk as he was very busy as director of the institute. But he

stayed late one evening to explain to me his results from his Japanese paper [5]. In this paper Masatoshi extended Ivan Cherednik's work on the affine Hecke algebraic interpretation of Macdonald polynomials to the setting of Koornwinder polynomials. I was eager to learn more about it, and I ended up studying the topic more closely after my Ph.D. Masatoshi and I decided that it was worthwhile to explain the Hecke algebraic perspective in full detail in the context of Askey-Wilson polynomials. The resulting joint paper [6] has recently gained new attention because of unexpected connections to quantum topology.

These were exciting times, in which the developments on quantum groups and Macdonald polynomials were taking place at a very fast pace. Masatoshi was a central figure in these developments, who inspired me and many other researchers with his work. For instance, his paper [3] is an important stepping stone in Gail Letzter's classification–free identification of Macdonald polynomials as spherical functions associated to quantum symmetric pairs. Unfortunately, Gail also passed away last year at a relatively young age [7].

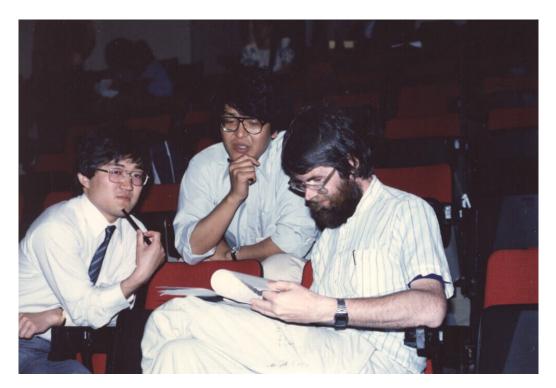


Figure 2: Koornwinder explaining his math to Noumi and Mimachi in Columbus, Ohio, May 1989.

It was always a great pleasure to meet Masatoshi and to talk to him. The last time I communicated with Masatoshi was a couple of years ago, after the online conference for my 50<sup>th</sup> birthday. Masatoshi wrote to me: "There are many things I would like to talk and discuss with you. I will think of visiting you in Amsterdam, hoping the pandemic situation will be settled in some way before the next summer. I also hope we will have a chance to work together in the nearest future." I wish I could turn back time and make this happen.

# Remembering Masatoshi Noumi

Tom Koornwinder (thkmath@xs4all.nl)

My first encounter with Noumi and Mimachi (Noumi's friend and coauthor) was at the NATO Advanced Study Institute *Orthogonal polynomials and their applications* held in Columbus, Ohio during May 22 -



Figure 3: Opdam, Koornwinder, Mimachi and Noumi in Ann Arbor, Michigan, June 1989.

June 3, 1989. There I presented my new result [8] on the interpretation of certain Askey-Wilson polynomials as spherical functions on quantum SU(2). This was a tough thing for me, on which I had labored until the last moment before my lecture. Noumi and Mimachi were very interested in my result because they were hunting for something similar, but still missed some essential ingredients of a proof. Later during the conference I explained my results to them in more detail (see Figure 2). This fell on fertile ground. Soon they published far reaching extensions [9] of my result. After the conference Noumi, Mimachi, Eric Opdam and I drove to Ann Arbor, Michigan, where we attended a *Regional Conference on Combinatorics and Algebra*, June 6–10, 1989. This was a most cheerful trip (see Figure 3).

Noumi visited Amsterdam several times. In 1994 he spent a few weeks there when mathematicians from several Dutch universities, collaborating in the Stieltjes Institute, got a major grant for inviting foreign experts. Then Noumi and I also played the recorder together and we even performed a Telemann canon sonata at a music evening organized by my Faculty at the University of Amsterdam. In August 2003 he spoke at a conference in Amsterdam on the occasion of my 60<sup>th</sup> birthday (see Figure 4).

My Ph.D. student Mathijs Dijkhuizen was a postdoc at Noumi's Univertsity in Kobe, Japan, and published there with Noumi on Macdonald-Koornwinder polynomials [2] as spherical functions on quantum groups [4]. Noumi published in 1995 a paper [5] in Japanese which prepared the road for Sahi's introduction [10] in 1999 of a nonsymmetric version of Macdonald-Koornwinder polynomials. For historical reasons it would be still worthwhile if an English translation of Noumi's paper could be made available.

Soon Noumi started working on Painlevé equations. His book *Painlevé equations through symmetry* (2000, in Japanese) appeared in 2004 with English translation [11]. He also did a lot of work on elliptic hypergeometric functions.

I attended a conference in March 2015 in Kyoto in honor of Noumi's 60<sup>th</sup> birthday. (This will probably remain my only visit to Japan.) During the conference dinner the birthday was celebrated with a typically Japanese ceremony (see Figure 5).

Noumi spent the academic year 2020-2021 in Stockholm, during covid, and in winter he gave there on-



Figure 4: Noumi lecturing in Amsterdam, August 2003 with Stokman listening.

line lectures on Macdonald polynomials, which I attended. They appeared in a book published in 2023 [12].

A dear friend and powerful mathematician has passed away. We will miss him.

\* \* \*

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- [3] M. Noumi, Macdonald's Symmetric polynomials as zonal spherical functions on some quantum homogeneous spaces, Advances in Mathematics, 123, 1 (1996), Pages 16-77.
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Figure 5: Noumi in his 60<sup>th</sup> birthday "chanchanko" outfit giving an after dinner speech in Kyoto, March 2015. According to Junichi Shiraishi in an email on March 3, 2025, in reference to this photo, he recalls: "at the time of Noumi's 60<sup>th</sup> birthday, Masatoshi compared his life of under 60 and over 60, to the side A and side B of a music record. Probably he wanted to recall to me the fact that some very good records have tremendously beautiful music on its B side, but remains not very much recognized among people unfortunately or fortunately. What he told me is totally correct. He continued to create and play deep music…"

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- [10] S. Sahi, Nonsymmetric Koornwinder polynomials and duality, Annals of Mathematics, **150** (1999), Pages 267–282.
- [11] M. Noumi, Painlevé equations through symmetry, Translations of Mathematical Monographs, 223 (2004), Translated from the 2000 Japanese original by the author, American Mathematical Society, Providence, RI, Pages x+156.

[12] M. Noumi, Macdonald polynomials: commuting family of q-difference operators and their joint eigenfunctions. Springer Briefs in Mathematical Physics, **50** (2023), Springer, Singapore, Pages viii+132.

From: Howard Cohl (howard.cohl@nist.gov)

Subject: Recollections of the Printed Newsletter for the SIAM Activity Group on OPSF (1990–2002)

First a bit of history (please see Tom Koornwinder's OP-SF NET archive https://staff.fnwi.uva.nl/t.h.koorn-winder/opsfnet/). OP-SF NET, the online Newsletter of SIAG/OPSF has been active since its first edition: Volume 1, Number 1, December 22, 1993. It started as a beautifully crafted ASCII text document (you really should read Volume 1, Number 1). Tom continued as sole editor until Volume 3, Number 2, March 14, 1996 when Martin Muldoon joined him as co-editor. Tom's last edition as co-editor with Martin was Volume 5, Number 6, November 15, 1998. OP-SF NET has maintained a frequency of six issues a year from the beginning.

Martin continued as sole editor until Volume 13, Number 1, January 15, 2006, where he was joined as co-editor by Diego Dominici. OP-SF NET transitioned from ASCII to pdf format in Volume 14, Number 3, May 15, 2007, while Martin and Diego were editors. Martin and Diego co-edited OP-SF NET until Volume 22, Number 1, January 15, 2015. At that point, Howard Cohl and Kerstin Jordaan co-edited the online Newsletter until Volume 23, Number 3, May 15, 2016 when Sarah Post joined as co-editor. The three of us co-edited the Newsletter until Volume 23, Number 6, November 15, 2016, at which point Kerstin stepped down as co-editor. Sarah and I have been co-editing the online Newsletter ever since.

It should be noted that from the Fall of 1990 until October 2002, there was also a nicely formatted, printed Newsletter for SIAG/OPSF! During that time there were 34 editions of this printed Newsletter in 13 volumes.

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• 1990: <del>1-1</del>.
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- 1991: **2-1**.
- 1992: 3-1, 3-2, 3-3, 3-4.
- 1993: 4-1, 4-2, 4-3, 4-4.
- 1994: 5-1, 5-2.
- 1995: 6-1, 6-2, 6-3.
- 1996: 7-1, 7-2, 7-3.
- 1997: 8-1, 8-2, 8-3.
- 1998: 9-1, 9-2, 9-3.
- 1999: 10-1, 10-2, 10-3.
- 2000: 11-1, 11-2, 11-3.
- 2001: 12-1, 12-2, 12-3.
- 2002: <del>13-1</del>.

The editors for this Newsletter:

- 1. George Gasper, Charles Dunkl (1-1, 2-1).
- 2. Eugene Tomer (3-1, ..., 5-2).
- 3. Wolfram Koepf (6-1, ..., 9-1).
- 4. Renato Álvarez Nodarse (8-3, ..., 12-3).

5. Rafael J. Yáñez (8-3, ..., 13-1).

Much appreciation to Wolfram Koepf for his assembling the online archive of scanned Newsletters! This Newsletter contains a lot of useful historical information including many contributions from Richard Askey. It's well-worth a read and scan.

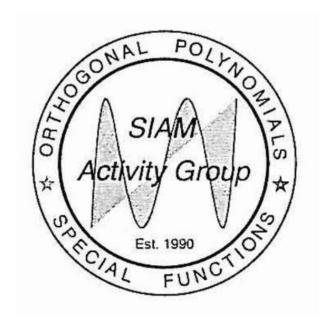


Figure 6: Eugene Tomer's design of the SIAG/OPSF logo.

According to Charles Dunkl in an email dated March 13, 2025:

Before the newsletter came the start of the SIAM SIAG/OPSF activity group. It took thirty signatures of SIAM members to get a group organized. I circulated the petition at the NATO Advanced Study Institute "Orthogonal polynomials and their applications" held at Ohio State University (Columbus, OH) in May 1989. I chatted with Seymour Parker who was SIAM president at the time about the process (I knew him from my time as a grad student at U. Wisconsin). It was a very good meeting. Ian Macdonald gave an impressive lecture—the organizers provided a grad student to erase the boards during his lecture—to keep up with the speed of his well–prepared (!!!) lecture. I met Herbert Stahl (no longer with us, I'm sorry to say) and some other German mathematicians.

I got the signatures and got going on the group. We needed officers besides me—I got George Gasper, Jet Wimp and Mourad Ismail on board. I approached Dick Askey—he politely suggested I get "younger people" for the job. Out of the blue I heard from Eugene Tomer who volunteered to produce the Newsletter. We hoped for 4–6 pages, it would be typed and then photocopied and printed by SIAM (all done by US mail). Eugene designed a logo (based on the graph of some low degree Chebyshev polynomials). [See Figure 6.] George Gasper had the idea of a problems section—as a side note, at the 1995 Workshop on "Special functions, q-series and related topics" at the Fields Institute in Toronto where George gave a series of lectures, which included homework problems for the younger people (grad students, for example) so setting problems for others is very much George's m.o. [modus operandi].

I communicated with Eugene exclusively by email—except for one time I met him in person at the annual SIAM meeting in Los Angeles—Century City (I recall?). For all the time that he was editor he did a great and careful job with the Newsletter. We invented the position of "appointed editor," rather than an elected officer—with the approval of SIAM. Eventually the position passed on to someone else (sorry, I don't remember). Later I was sorry to hear

about his passing—when the American Astronomical Society asked me to write an obituary for Eugene—apparently no astronomer knew him well enough. Evidently among his interest—besides amateur radio—was astronomy. I would say that my emphases were on that he freely gave of his time and energy to support the activity group, and that he strongly wanted us to contribute to worthwhile applications of special functions in the real world. It is true for many of us academics (like me) that we are insulated from the non–university work in mathematics, and it was a privilege for me to interact with someone like Eugene Tomer.

According to George Gasper in an email dated February 12, 2025:

While I was Secretary (1990–1992) of the SIAM Activity Group on Orthogonal Polynomials and Special Functions. I assisted Charles Dunkl (who was Chair of SIAG/OPSF) in editing the SIAG/OPSF Printed Newsletters for the Fall of 1990 (1–1, 2 pages) and 1991 (Vol. 2–1, 3 pages). The Newsletters covered reports of recent and upcoming meetings, current books of interest, editorial notes, etc.

With the growth of the activity group and length of the Newsletter, I was glad that Eugene Tomer volunteered to edit the Newsletter and started editing it in July of 1992. The Fall 1992 (Vol. 3–1) Newsletter turned out to be 8 pages (in double columns) long, including a 3 page Membership Directory of 115 members. Also, since Eugene and I were both amateur radio operators (with call signs WI6X and KK9X, respectively), we enjoyed adding comments about it at the ends of our Newsletter related emails.

When Eugene started editing the Newsletter he added a Problems section and requested the submission of new problems for it. My submitted problem concerning the convexity of a certain multiple of a hypergeometric series turned out be Problem 2 in the Fall 1992 (Vol. 3-1) Newsletter. Since Problem 2 hadn't been solved by 1996, Dick Askey and I submitted a solution to it, which appeared on pages 18–19 of the Oct. 1997 (Vol. 8–1) issue. Problem 19. Uniform Bounds for Shifted Jacobi Multiplier Sequences (by George Gasper and Walter Trebels), which is in the June 1998 (Vol. 8–3, pp. 11–12) Newsletter, is still unsolved.

Eugene Tomer passed away on 2 July 2007 at his home in San Francisco, California. Charles Dunkl has written an obituary for Eugene Tomer in the BAAS (Bulletin of the American Astronomical Society). In that obituary, he says about Eugene Tomer regarding his editorship of the printed SIAG/OPSF Newsletter (Bulletin of the American Astronomical Society (BAAS, Volume 41, Issue 1, Obituary):

...This writer met Eugene at the 1992 Annual SIAM meeting in Los Angeles in connection with the Activity Group on Orthogonal Polynomials and Special Functions, which the writer chaired at the time. Eugene volunteered to edit the Newsletter of the group, which he did from July 1992 to July 1995. Thanks to his skills and efforts, the Newsletter became a carefully edited, professional publication. Eugene not only organized a Problems Column, attracting questions in pure and applied mathematics, but he also designed the logo for the group. He gave much time and effort to this service, in an era when copy had to be physically assembled and mailed to SIAM Headquarters. Eventually he felt he had done what he could for the Activity Group. He told me that he hoped the Group would get seriously involved with applications such as in astronomy, physics, and sciences that use special function solutions of differential equations.

During Tomer's editorship, we communicated mostly by e-mail, our homes being far apart. He was a good friend to the Group and to me, as much as one can be over a separation of thousands of miles. As well, Eugene was an active amateur radio operator, much appreciated by his local amateur radio community, with call sign WI6X.

According to Wolfram Koepf in an email of January 1, 2025:

Eugene Tomer was the first Editor of the Newsletter, and he resigned in 1995. The officers of the SIAM activity group OPSF – at that time Charles Dunkl, George Gasper, Martin Muldoon and Tom Koornwinder – asked urgently, who would be willing to continue, and I was interested

and responded positively. As a result they appointed me, and I started with issue 6-1. You can read everything about this transition in issue 6-1.

I didn't know Eugene Tomer personally, but I had email contact with him and he sent me his files. I found the editing process which was also new for me very interesting! However, I had written already several books before so the editing process was not completely new to me. For me it was clear from the beginning that I would like to do this job for three years or so, and therefore I stopped by asking for somebody to continue. I don't really remember anything about my transition to stopping being an editor of the printed Newsletter. Renato Álvarez Nodarse and Rafael J. Yáñez agreed, we did issue 8–3 together, afterwards they took over. I absolutely enjoyed my time being an Editor for the Newsletter!

According to Renato Álvarez Nodarse in an email on January 1, 2025:

Wolfram Koepf was the editor before I was, he contacted me and suggested that I become editor. In fact I (and Rafael J. Yáñez, a colleague from Granada) edited one or two Newsletters with Koepf before we started to edit alone! I enjoyed being an editor for the Newsletter, but it was a lot of work! I recall that SIAM decided that printing and shipping was very expensive and therefore the printed version should be canceled out.

Topic #7 — OP - SF Net 32.2 — March 15, 2025

From: OP-SF Net Editors Subject: Preprints in arXiv.org

The following preprints related to the fields of orthogonal polynomials and special functions were posted or cross-listed to one of the subcategories of arXiv.org during January and February 2025. This list has been separated into two categories.

# **OP-SF Net Subscriber E-Prints**

#### http://arxiv.org/abs/2501.01408

Quantum periods, toric degenerations and intrinsic mirror symmetry Sam Johnston

### http://arxiv.org/abs/2501.02877

Multi-indexed Orthogonal Polynomials of a Discrete Variable and Exactly Solvable Birth and Death Processes

Satoru Odake

#### http://arxiv.org/abs/2501.03234

Theorems and Conjectures on an Arithmetic Sum Associated with the Classical Theta Function  $\theta_3$  Bruce C. Berndt, Raghavendra N. Bhat, Jeffrey L. Meyer, Likun Xie, Alexandru Zaharescu

#### http://arxiv.org/abs/2501.03918

On generalized Mittag-Leffler-type functions of two variables Anvar Hasanov, Erkinjon Karimov

#### http://arxiv.org/abs/2501.05696

Combinatorial identities related to degenerate Stirling numbers of the second kind Taekyun Kim, Dae san Kim

Rank, two-color partitions and Mock theta function George E. Andrews, Rahul Kumar

#### http://arxiv.org/abs/2501.07144

Dualities in random matrix theory

Peter J. Forrester

# http://arxiv.org/abs/2501.09626

Refinements of Van Hamme's (E.2) and (F.2) supercongruences and two supercongruences by Swisher Victor J. W. Guo, Chen Wang

#### http://arxiv.org/abs/2501.12197

Inequalities for an integral involving the modified Bessel function of the first kind Robert E. Gaunt

#### http://arxiv.org/abs/2501.12413

The Laguerre constellation of classical orthogonal Polynomials Roberto S. Costas-Santos

#### http://arxiv.org/abs/2501.12679

The multiplicative constant in asymptotics of higher-order analogues of the Tracy-Widom distribution Dan Dai, Wen-Gao Long, Shuai-Xia Xu, Lu-Ming Yao, Lun Zhang

#### http://arxiv.org/abs/2501.12806

Bispectrality of the sieved Jacobi polynomials Luc Vinet, Alexei Zhedanov

#### http://arxiv.org/abs/2501.13330

Hypergeometric Distributions and Joint Families of Elliptic Curves Brian Grove, Hasan Saad

#### http://arxiv.org/abs/2501.15287

Some examples of orthogonal matrix polynomials satisfying odd order differential equations Antonio J. Durán, Manuel D. De la Iglesia

#### http://arxiv.org/abs/2501.15294

Matrix valued orthogonal polynomials related to SU(N+1), their algebras of differential operators and the corresponding curves

F. Alberto Grünbaum, Manuel D. De la Iglesia

#### http://arxiv.org/abs/2501.17291

Polyanalytic Hermite polynomials associated with the elliptic Ginibre model Nizar Demni, Zouhaïr Mouayn

#### http://arxiv.org/abs/2501.17710

Approximation of Askey-Wilson roots Jan Felipe van Diejen, Andrés Soledispa, Adrián Vidal

#### http://arxiv.org/abs/2502.00166

A unified approach to hypergeometric class functions lan Dereziński

Dirichlet Species and Arithmetic Zeta Functions John C. Baez

# http://arxiv.org/abs/2502.02419

On a function of Ramanujan twisted by a logarithm Atul Dixit, Sumukha Sathyanarayana, N. Guru Sharan

#### http://arxiv.org/abs/2502.02432

Some topological genera and Jacobi forms Tewodros Amdeberhan, Michael Griffin, Ken Ono

#### http://arxiv.org/abs/2502.03074

On string functions of the generalized parafermionic theories, mock theta functions, and false theta functions, II

Nikolay Borozenets, Eric T. Mortenson

# http://arxiv.org/abs/2502.04275

Algebras behind the bispectrality of the Wilson rational functions and their  $_4\varphi_3$  limits Nicolas Crampé, Satoshi Tsujimoto, Luc Vinet, Alexei Zhedanov

#### http://arxiv.org/abs/2502.04962

Special Functions from a Complex Viewpoint Henrik Laurberg Pedersen

# http://arxiv.org/abs/2502.04992

The multiple Markov theorem on Angelesco sets K. Castillo, G. Gordillo-Núñez

#### http://arxiv.org/abs/2502.06384

Polynomially Superintegrable Hamiltonians Separating in Cartesian Coordinates Ian Marquette, Anthony Parr

#### http://arxiv.org/abs/2502.07142

Moments of characteristic polynomials for classical  $\beta$  ensembles Bo-Jian Shen, Peter J. Forrester

# http://arxiv.org/abs/2502.09259

Arithmetic properties of the Taylor coefficients of differentially algebraic power series Christian Krattenthaler, Tanguy Rivoal

#### http://arxiv.org/abs/2502.11424

Bounds for weighted Chebyshev and residual polynomials on subsets of  $\mathbb R$  Jacob S. Christiansen, Barry Simon, Maxim Zinchenko

#### http://arxiv.org/abs/2502.11988

Nice q-analogs of orthogonal polynomials with nice moments: Some simple examples Johann Cigler

# http://arxiv.org/abs/2502.12709

Dynamic generalizations of the Asymmetric Inclusion Process, Asymmetric Brownian Energy Process and their Dualities Carel Wagenaar

Asymptotics of  $L^r$  extremal polynomials for  $0 < r \le \infty$  on  $C^{1+}$  Jordan regions Benedikt Buchecker, Benjamin Eichinger, Maxim Zinchenko

#### http://arxiv.org/abs/2502.19096

Counting domino and lozenge tilings of reduced domains with Padé-type approximants Christophe Charlier, Tom Claeys

### http://arxiv.org/abs/2502.19309

Rogers-Ramanujan Type Identities for Rank Two Partial Nahm Sums Liuquan Wang, Wentao Zeng

# http://arxiv.org/abs/2502.19326

Matrix Bessel Biorthogonal Polynomials: A Riemann-Hilbert approach Amílcar Branquinho, Ana Foulquié-Moreno, Assil Fradi, Manuel Mañas

# http://arxiv.org/abs/2502.20813

Infinite-dimensional q-Jacobi Markov processes Grigori Olshanski

# Other Relevant OP-SF E-Prints

# http://arxiv.org/abs/2501.01265

Signs of high order derivatives for the theta and Epstein zeta functions and application Deng Kaixin, Luo Senping

# http://arxiv.org/abs/2501.01364

Two characterizations of Sheffer-Dunkl sequences Alejandro Gil Asensi, Judit Minguez Ceniceros

#### http://arxiv.org/abs/2501.01380

The Mordell-Tornheim zeta function: Kronecker limit type formula, Series Evaluations and Applications Sumukha Sathyanarayana, N. Guru Sharan

#### http://arxiv.org/abs/2501.01419

Riemann-Hilbert problems, Fredholm determinants, explicit combinatorial expansions, and connection formulas for the general q-Painlevé  $\mathrm{III}_3$  tau functions Pavlo Gavrylenko

# http://arxiv.org/abs/2501.02145

Approximation by polynomials with only real critical points David L. Bishop

#### http://arxiv.org/abs/2501.02358

Chebyshev systems and Sturm oscillation theory for discrete polynomials D. V. Gorbachev, V. I. Ivanov, S. Yu. Tikhonov

# http://arxiv.org/abs/2501.02377

Embedding integrable spin models in solvable vertex models on the square lattice M. J. Martins

On Large-Space and Long-Time Asymptotic Behaviors of Kink-Soliton Gases in the Sine-Gordon Equation Guogiang Zhang, Weifang Weng, Zhenya Yan

# http://arxiv.org/abs/2501.03623

Approximations by special values of multiple cosine and sine functions Su Hu, Min-Soo Kim

# http://arxiv.org/abs/2501.03646

Jacob's ladders and new equivalents of the Fermat-Wiles theorem connected with some cross-bred of the formulae of Hardy-Littlewood-Ingham (1926) and of Ingham (1926) Jan Moser

#### http://arxiv.org/abs/2501.03774

Reduction of bielliptic hyperelliptic functions of genus 3 Takanori Ayano

# http://arxiv.org/abs/2501.04703

Chebyshev polynomials involved in the Householder's method for square roots Yann Dijoux

# http://arxiv.org/abs/2501.05027

Zeta function of F-gauges and special values Shubhodip Mondal

#### http://arxiv.org/abs/2501.05321

A note on the number of irrational odd zeta values, II Li Lai

# http://arxiv.org/abs/2501.05773

Simulations of multivariate gamma distributions and multifactor gamma distributions Philippe Bernardoff, Bénédicte Puig

#### http://arxiv.org/abs/2501.05860

Multidimensional moment problem and Stieltjes transform Ivan Kovalyov

# http://arxiv.org/abs/2501.06195

Deformed Boson Algebras and  $\mathcal{W}_{\alpha,\beta,\nu}$ -Coherent States: A New Quantum Framework Riccardo Droghei

#### http://arxiv.org/abs/2501.06206

 $_3F_4$  hypergeometric functions as a sum of a product of  $_2F_3$  functions Jack C. Straton

#### http://arxiv.org/abs/2501.06886

Integrals of Legendre polynomials and approximations Abdelhamid Rehouma

#### http://arxiv.org/abs/2501.07241

Segal-Bargmann transforms and generalized Weyl algebras associated with the Meixner class of orthogonal polynomials

Chadaphorn Kodsueb, Eugene Lytvynov

Relating flat connections and polylogarithms on higher genus Riemann surfaces Eric D'Hoker, Benjamin Enriquez, Oliver Schlotterer, Federico Zerbini

#### http://arxiv.org/abs/2501.08310

Variations on hypergeometric functions Michał Zakrzewski, Henryk Żołądek

#### http://arxiv.org/abs/2501.10076

Accurate algorithms for Bessel matrices Jorge Delgado, Héctor Orera, Juan Manuel Peña

#### http://arxiv.org/abs/2501.10109

Generalizations of two hypergeometric sums related to conjectures of Guo Arijit Jana, Liton Karmakar

# http://arxiv.org/abs/2501.10238

Stationary solutions with vacuum for a hyperbolic-parabolic chemotaxis model in dimension two Sophia Hertrich, Tao Huang, Diego Yépez, Kun Zhao

#### http://arxiv.org/abs/2501.10397

Polynomial potential minimization on the unit circle Josiah Park

# http://arxiv.org/abs/2501.10545

Sesquilinear forms as eigenvectors in quasi \*-algebras, with an application to ladder elements Fabio Bagarello, Hiroshi Inoue, Salvatore Triolo

#### http://arxiv.org/abs/2501.10795

Poncelet pairs of a circle and parabolas from a confocal family and Painlevé VI equations Vladimir Dragović, Mohammad Hassan Murad

#### http://arxiv.org/abs/2501.11033

A Littlewood-Paley approach to the Mittag-Leffler function in the frequency space and applications to nonlocal problems

Ahmed A. Abdelhakim

# http://arxiv.org/abs/2501.11092

On Gegenbauer polynomials and Wronskian determinants of trigonometric functions Minjian Yuan

#### http://arxiv.org/abs/2501.11303

New Proofs of the Explicit Formulas of Arakawa-Kaneko Zeta Values and Kaneko-Tsumura  $\eta$ - and  $\psi$ - Values

Masanobu Kaneko, Weiping Wang, Ce Xu, Jiangiang Zhao

# http://arxiv.org/abs/2501.12105

The density conjecture for Juddian points for the quantum Rabi model Rishi Kumar, Zeév Rudnick

Bilateral Bailey pairs and Rogers-Ramanujan type identities Xiangxin Liu, Lisa Hui Sun

#### http://arxiv.org/abs/2501.14422

Mesoscopic Edge Universality of Orthogonal Polynomial Ensembles Wenkui Liu

# http://arxiv.org/abs/2501.14545

Pair Correlation of Zeros of the Riemann Zeta Function I: Proportions of Simple Zeros and Critical Zeros Siegfred Alan C. Baluyot, Daniel Alan Goldston, Ade Irma Suriajaya, Caroline L. Turnage-Butterbaugh

#### http://arxiv.org/abs/2501.14714

Super-Hamiltonians for super-Macdonald polynomials Dmitry Galakhov, Alexei Morozov, Nikita Tselousov

#### http://arxiv.org/abs/2501.15241

Optimal result involving the Green's function Zakaria Boucheche

#### http://arxiv.org/abs/2501.15277

Characterizing the Lovasz theta function via walk generating functions Lasse Harboe Wolff

# http://arxiv.org/abs/2501.15866

On the location of the complex conjugate zeros of the partial theta function Vladimir Petrov Kostov

#### http://arxiv.org/abs/2501.16478

Polynomial sequences with the same recurrence relation as Chebyshev polynomials and the minimal polynomial of  $2\cos(2\pi/n)$ 

Mamoru Doi

# http://arxiv.org/abs/2501.16746

Hard to soft edge transition for the Muttalib-Borodin ensembles with integer parameter  $\theta$  Dong Wang, Shuai-Xia Xu

# http://arxiv.org/abs/2501.16779

New exponent pairs, zero density estimates, and zero additive energy estimates: a systematic approach Terence Tao, Tim Trudgian, Andrew Yang

#### http://arxiv.org/abs/2501.17516

Stokes Phenomenon and Yangians

Qian Tang, Xiaomeng Xu

#### http://arxiv.org/abs/2501.17765

Domino Tilings, Domino Shuffling, and the Nabla Operator Ian Cavey, Yi-Lin Lee

#### http://arxiv.org/abs/2501.17956

The Numerical Approximation of Caputo Fractional Derivative of Higher Orders Using A Shifted Gegenbauer Pseudospectral Method: Two-Point Boundary Value Problems of the Bagley Torvik Type Case Study Kareem T. Elgindy

Periodicity and absolute zeta functions of multi-state Grover walks on cycles Jirô Akahori, Norio Konno, Iwao Sato, Yuma Tamura

#### http://arxiv.org/abs/2502.00254

Even Hypergeometric Polynomials and Finite Free Commutators Jacob Campbell, Rafael Morales, Daniel Perales

### http://arxiv.org/abs/2502.00303

Representation of solutions of the one-dimensional Dirac equation in terms of Neumann series of Bessel functions

Emmanuel Roque, Sergii M. Torba

# http://arxiv.org/abs/2502.00335

Asymptotics for multiple q-orthogonal polynomials from the RHP Tomas Lasic Latimer

# http://arxiv.org/abs/2502.00478

Orthogonality of spin q-Whittaker polynomials Matteo Mucciconi

# http://arxiv.org/abs/2502.00624

Expressing the difference of two Hurwitz zeta functions by a linear combination of the Gauss hypergeometric functions
Feng Qi

#### http://arxiv.org/abs/2502.01109

Geometric Gauss Sums and Gross-Koblitz Formulas over Function Fields Ting-Wei Chang

#### http://arxiv.org/abs/2502.01288

On an unconditional  $GL_3$  analog of Selberg's result Qingfeng Sun, Hui Wang

#### http://arxiv.org/abs/2502.01363

Generalized Counting Process with Random Drift and Different Brownian Clocks Mostafizar Khandakar, Manisha Dhillon, Kuldeep Kumar Kataria

# http://arxiv.org/abs/2502.01369

On the extremal eigenvalues of Jacobi ensembles at zero temperature Kilian Hermann, Michael Voit

# http://arxiv.org/abs/2502.01415

The Fibonacci Zeta Function and Modular Forms
Eran Assaf, Chan leong Kuan, David Lowry-Duda, Alexander Walker

#### http://arxiv.org/abs/2502.01499

Refined Painlevé/gauge theory correspondence and quantum tau functions G. Bonelli, A. Shchechkin, A. Tanzini

Lifespan estimate for the semilinear regular Euler-Poisson-Darboux-Tricomi equation Yuequn Li, Fei Guo

#### http://arxiv.org/abs/2502.02089

Implicit integration factor method coupled with Padé approximation strategy for nonlocal Allen-Cahn equation

Yuxin Zhang, Hengfei Ding

### http://arxiv.org/abs/2502.02147

On Siegel's problem and Dwork's conjecture for G-functions Javier Fresán, Yeuk Hay Joshua Lam, Yichen Qin

# http://arxiv.org/abs/2502.02273

Long-time asymptotics for the  $N_\infty$ -soliton solution to the KdV equation with two types of generalized reflection coefficients Guoqiang Zhang, Zhenya Yan

#### http://arxiv.org/abs/2502.02604

A novel construction of Jacobi's elliptic functions from deformed Lie algebra Arindam Chakraborty

#### http://arxiv.org/abs/2502.02776

On Transformation properties of hypergeometric motives and Diophantine equations Ariel Pacetti

# http://arxiv.org/abs/2502.02819

Can one hear the shape of a crystal? Haina Wang, Salvatore Torquato

#### http://arxiv.org/abs/2502.03276

High-precision numerical evaluation of Lauricella functions M.A. Bezuglov, B.A. Kniehl, A.I. Onishchenko, O.L. Veretin

#### http://arxiv.org/abs/2502.03374

An explicitly solvable NLS model with discontinuous standing waves Riccardo Adami, Filippo Boni, Takaaki Nakamura, Alice Ruighi

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Cheap and stable quadrature on polyhedral elements Alvise Sommariva, Marco Vianello

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Multiplicativity of Fourier Coefficients of Maass Forms for  $SL(n, \mathbb{Z})$  Dorian Goldfeld, Eric Stade, Michael Woodbury

#### http://arxiv.org/abs/2502.03842

A note on order estimates of the q-analogue of the Riemann zeta function Hideki Murahara, Tomokazu Onozuka

#### http://arxiv.org/abs/2502.03880

Uniqueness and explicit form of linear Hermite-Chebyshev approximations A. P. Starovoitov, I. V. Kruglikov

Maximum Likelihood Estimation of the Parameters of Matrix Variate Symmetric Laplace Distribution Pooja Yadav, Tanuja Srivastava

#### http://arxiv.org/abs/2502.04150

How large are the gaps in phase space? Michael Speckbacher

# http://arxiv.org/abs/2502.04608

Algebraic cycles and values of Green's functions I- Products of Elliptic Curves Ramesh Sreekantan (with an appendix by Kannappan Sampath)

#### http://arxiv.org/abs/2502.04731

Congruence properties of prime sums and Bernoulli polynomials Jean-Christophe Pain

# http://arxiv.org/abs/2502.05022

On a suspension formula for Denef-Loeser zeta functions E. Artal Bartolo, P. D. González Pérez, M. González Villa, E. León-Cardenal

# http://arxiv.org/abs/2502.05106

Fourier optimization and pair correlation problems Mithun Kumar Das, Tolibjon Ismoilov, Antonio Pedro Ramos

# http://arxiv.org/abs/2502.05134

Information-Theoretic Guarantees for Recovering Low-Rank Tensors from Symmetric Rank-One Measurements

Eren C. Kızıldağ

#### http://arxiv.org/abs/2502.05366

An effective estimation of multivariate density functions using extended-beta kernels with Bayesian adaptive bandwidths

Sobom M. Somé, Célestin C. Kokonendji, Francial G.B. Libengué Dobélé-Kpoka

#### http://arxiv.org/abs/2502.05455

Exactly solvable multicomponent spinless fermions Ryu Sasaki

# http://arxiv.org/abs/2502.05507

Unfitted boundary algebraic equation method based on difference potentials and lattice Green's function in 3D

Qing Xia

# http://arxiv.org/abs/2502.05861

Some characterizations of weak left braces Shoufeng Wang

# http://arxiv.org/abs/2502.05886

An estimate for  $\beta$ -Hermite ensembles via the zeros of Hermite polynomials Michael Voit

On the quasi-uniformity properties of quasi-Monte Carlo lattice point sets and sequences Josef Dick, Takashi Goda, Gerhard Larcher, Friedrich Pillichshammer, Kosuke Suzuki

#### http://arxiv.org/abs/2502.06449

Denominator identity for the affine Lie superalgebra  $\widehat{\mathfrak{spo}}(2m,2m+1)$  and indefinite theta functions Toshiki Matsusaka, Miyu Suzuki

# http://arxiv.org/abs/2502.06506

Certain Weighted  $L^p$ -improving estimates for the totally-geodesic k-plane transform on simply connected spaces of constant curvature Aniruddha Deshmukh, Ashisha Kumar

#### http://arxiv.org/abs/2502.08305

On additive convolution sum of arithmetic functions and related questions Bikram Misra, Biswajyoti Saha, Anubhav Sharma

# http://arxiv.org/abs/2502.08760

Modular Forms and Certain  ${}_2F_1(1)$  Hypergeometric Series Esme Rosen

# http://arxiv.org/abs/2502.09072

Noncommutative chromatic quasi-symmetric functions, Macdonald polynomials, and the Yang-Baxter equation

Jean-Christophe Novelli, Jean-Yves Thibon

# http://arxiv.org/abs/2502.09852

On the mean values of the Barnes multiple zeta function Takashi Miyagawa, Hideki Murahara

#### http://arxiv.org/abs/2502.10483

A class of positive Fox H-functions Filippo Giraldi

#### http://arxiv.org/abs/2502.10885

A series of definite integrals involving upper incomplete Gamma functions Matyas Barczy, István Mező

#### http://arxiv.org/abs/2502.10965

Higher Rank Macdonald Polynomials Milo Bechtloff Weising

#### http://arxiv.org/abs/2502.11815

A purely analytic derivation of Bonnet surfaces Robert Conte, A. Michel Grundland

#### http://arxiv.org/abs/2502.11852

Algebraic Independence of an Airy Function, Its Derivative, and an Antiderivative Folkmar Bornemann

#### http://arxiv.org/abs/2502.11914

Positive Biorthogonal Curvature on  $S^2 \times T^2$ : An open problem no more? Alexander Pigazzini

pylevin: efficient numerical integration of integrals containing up to three Bessel functions Robert Reischke

# http://arxiv.org/abs/2502.12268

Friedman-Ramanujan functions in random hyperbolic geometry and application to spectral gaps II Nalini Anantharaman, Laura Monk

#### http://arxiv.org/abs/2502.12410

Nonlinear wave solution to a coupled mKdV equations with variable coefficients Wenjuan Wu

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Network visualisations related to special functions based on the Scopus data since 1940 Rushan Ziatdinov

# http://arxiv.org/abs/2502.13098

Discrete N-particle systems at high temperature through Jack generating functions Cesar Cuenca, Maciej Dołęga

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Pseudo-involutions in the Riordan group and Chebyshev polynomials Alexander Burstein, Louis W. Shapiro

#### http://arxiv.org/abs/2502.13937

Vertex functions of type D Nakajima quiver varieties Hunter Dinkins, Jiwu Jang

#### http://arxiv.org/abs/2502.14295

Fusion rules and structure constants of E-series minimal models Rongvoram Nivesvivat, Sylvain Ribault

#### http://arxiv.org/abs/2502.14390

Hardy-Littlewood maximal, generalized Bessel-Riesz and generalized fractional integral operators in generalized Morrey and  $BMO_{\varphi}$  spaces associated with Dunkl operator on the real line Sumit Parashar, Saswata Adhikari

#### http://arxiv.org/abs/2502.14396

Fully spectral scheme for the linear BGK equation on the whole space Bastien Grosse

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Approximate roots
Patrick Popescu-Pampu

#### http://arxiv.org/abs/2502.14589

Explicit adaptive time stepping for the Cahn-Hilliard equation by exponential Krylov subspace and Chebyshev polynomial methods

Mike A. Botchev

Accurate analytic approximation for a fractional differential equation with a modified Bessel function term Byron Droguett, Pablo Martin, Eduardo Rojas, Jorge Olivares

#### http://arxiv.org/abs/2502.14876

Definite integrals involving Bessel functions expressed as a series of special functions Robert Reynolds

#### http://arxiv.org/abs/2502.15103

Global branching of solutions to ODEs and integrability Rod Halburd

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Mixed Berndt-Type Integrals and Generalized Barnes Multiple Zeta Functions Jianing Zhou

#### http://arxiv.org/abs/2502.15207

Sign changes in Fourier coefficients of the symmetric power L-functions on sums of two squares Amrinder Kaur

#### http://arxiv.org/abs/2502.15249

Three-parameter generalizations of formulas due to Guillera John M. Campbell

#### http://arxiv.org/abs/2502.15326

Feynman integrals, elliptic integrals and two-parameter K3 surfaces Claude Duhr, Sara Maggio

#### http://arxiv.org/abs/2502.15364

Universality of the zeta function in short intervals Yoonbok Lee, Łukasz Pańkowski

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Massive vector field perturbations in the Schwarzschild spacetime from supersymmetric gauge theory Xian-Hui Ge, Masataka Matsumoto, Kilar Zhang

#### http://arxiv.org/abs/2502.15852

On some properties of special functions involving k-gamma and k-digamma functions Li Yin, Jumei Zhang

#### http://arxiv.org/abs/2502.15892

Sharp Estimates for Large N Weingarten Functions Ron Nissim

#### http://arxiv.org/abs/2502.15966

Sums of Powers of Sine and Generalized Bernoulli Polynomials Leon D. Fairbanks

#### http://arxiv.org/abs/2502.16015

On the computation of the cumulative distribution function of the Normal Inverse Gaussian distribution Guillermo Navas-Palencia

The shifted convolution problem in function fields Alexandra Florea, Matilde Lalín, Amita Malik, Anurag Sahay

# http://arxiv.org/abs/2502.16070

Structure of operator algebras for matrix orthogonal polynomials Ignacio Bono Parisi, Inés Pacharoni

#### http://arxiv.org/abs/2502.16393

Inverse scattering transform for the defocusing local-and-nonlocal nonlinear Schrödinger equation with non-zero boundary conditions Chuanxin Xu, Tao Xu, Min Li

#### http://arxiv.org/abs/2502.16635

Riemann-Hilbert problems for bi-axially symmetric null-solutions to iterated perturbed Dirac equations in  $\mathbb{R}^n$ 

Dian Zuo, Min Ku, Fuli He

#### http://arxiv.org/abs/2502.16929

On the functional Minkowski problem

Tomer Falah, Liran Rotem

# http://arxiv.org/abs/2502.17008

Expression of special stretched 9j coefficients in terms of  ${}_5F_4$  hypergeometric series Jean-Christophe Pain

#### http://arxiv.org/abs/2502.17117

An Alternative Generating Function for k-Regular Partitions Kağan Kurşungöz

#### http://arxiv.org/abs/2502.17656

High-Q, size-independent, and reconfigurable optical antennas via zero-index material dispersion engineering

Prasad P. Iyer, Mihir Pendharkar, Anchal Agrawal, Humberto Foronda, Mike Iza, Umesh K. Mishra, Shuji Nakamura, Steven DenBaars, Stacia Keller, Chris Palmstrøm, Jon A. Schuller

#### http://arxiv.org/abs/2502.17884

The fractional Riesz transform and their commutator in Dunkl setting Yanping Chen, Xueting Han, Liangchuan Wu

#### http://arxiv.org/abs/2502.18896

A notion of fractality for a class of states and noncommutative relative distance zeta functional Yat Tin Chow

# http://arxiv.org/abs/2502.18921

Calogero-Sutherland-type quantum systems, generalized hypergeometric functions and superintegrability for integral chain

Fan Liu, Rui Wang, Jie Yang, Wei-Zhong Zhao

# http://arxiv.org/abs/2502.19084

On the surjectivity of p-adic Galois representations attached to Drinfeld modules of rank 2 Narasimha Kumar, Dwipanjana Shit

Quantum spherical functions of type  $\chi$  as Macdonald-Koornwinder polynomials Stein Meereboer

#### http://arxiv.org/abs/2502.19408

Enumerative Geometry of Quantum Periods Tim Gräfnitz, Helge Ruddat, Eric Zaslow, Benjamin Zhou

# http://arxiv.org/abs/2502.20109

New q-identities Via q-Derivative of Basic Hypergeometric Series with Respect to Parameters Ronald Orozco López

# http://arxiv.org/abs/2502.20302

Finite Fourier series. The class of trigonometric splines Volodymyr Denysiuk, Lydmila Rybachuk

# http://arxiv.org/abs/2502.20644

Recent advances about the rigorous integration of parabolic PDEs via fully spectral Fourier-Chebyshev expansions

Matthieu Cadiot, Jean-Philippe Lessard

# http://arxiv.org/abs/2502.20910

On Diophantine properties for values of Dedekind zeta functions Jerson Caro, Fabien Pazuki, Riccardo Pengo

Topic #8 — OP - SF Net 32.2 — March 15, 2025

From: OP-SF Net Editors

Subject: Submitting contributions to OP-SF NET and SIAM-OPSF (OP-SF Talk)

To contribute a news item to OP-SF NET, send e-mail to one of the OP-SF Editors howard.cohl@nist.gov, or spost@hawaii.edu.

Contributions to OP-SF NET 32.3 should be sent by May 1, 2025.

OP-SF NET is the electronic newsletter of the SIAM Activity Group on Special Functions and Orthogonal Polynomials (SIAG/OPSF). We disseminate your contributions on anything of interest to the special functions and orthogonal polynomials community. This includes announcements of conferences, forthcoming books, new software, electronic archives, research questions, and job openings as well as news about new appointments, promotions, research visitors, awards and prizes. OP-SF Net is transmitted periodically through a post to OP-SF Talk which is currently managed and moderated by Howard Cohl (howard.cohl@nist.gov). Anyone wishing to be included in the mailing list (SIAG/OPSF members and non-members alike) should send an email expressing interest to him. Bonita Saunders also posts the Newsletter through SIAM Engage (SIAG/OPSF) which is received by all SIAG/OPSF members.

OP-SF Talk is a listserv associated with SIAG/OPSF which facilitates communication among members, non-members and friends of the Activity Group. To post an item to the listserv, send e-mail to howard.cohl@nist.gov.

WWW home page of this Activity Group:

http://math.nist.gov/opsf

Information on joining SIAM and this activity group: service@siam.org

The elected Officers of the Activity Group (2025–2027) are:

Howard Cohl, Chair Kerstin Jordaan, Program Director Tom Trogdon, Secretary

The appointed officers are:

Howard Cohl, OP-SF NET co-editor
Sarah Post, OP-SF NET co-editor
Popita Saundars, Wohmaster and SIAM Engage (SIA)

Bonita Saunders, Webmaster and SIAM Engage (SIAG/OPSF) moderator

Topic #9 — OP – SF Net 32.2 — March 15, 2025

From: OP-SF Net Editors

Subject: Thought of the Month by Noumi

"The four parameter family of Askey-Wilson polynomials has played an important and central role in the theory of basic hypergeometric orthogonal polynomials. In fact, up to date they seem to be the most general family of basic hypergeometric orthogonal polynomials which satisfy the additional requirement that they are joint eigenfunctions of a second-order q-difference operator. We use the link between the Askey-Wilson polynomials and the most general non-reduced affine root system of rank one to derive in this paper the basic properties of the Askey-Wilson polynomials (and more!) from the algebraic structure of the associated (double) affine Hecke algebra."

**Masatoshi Noumi** (1955–2024), *Askey-Wilson polynomials: An affine Hecke algebraic approach*, Masatoshi Noumi and Jasper V. Stokman, Advances in the Theory of Special Functions and Orthogonal Polynomials, Nova Science Publishers, Inc., Hauppauge, NY, 2004, Pages 111–144.